

Data analysis – reserve: solution

Picture scale:

For example from stars C D > distance on picture = 63 ± 1 mm

From parallax triangle or from map measurements distance C-D = $2.5^\circ = 150'$

Scale $150'/63 = 2.38'/\text{mm} \approx 0.04^\circ/\text{mm}$

Comet's Head size = 7 mm = 0.28°

Comet's tail size (end of tail should be marked by student) 50 mm = 2° (angle HET)

Coordinates of comet $\alpha_1 \approx 21^{\text{h}}52'$ $\delta_1 \approx 37.5^\circ$; $\alpha_2 \approx 22^{\text{h}}03'$ $\delta_2 \approx 38.8^\circ$

Angular speed $\approx 2.5^\circ/24\text{h} = 6.25'/\text{h}$

Elongation ϵ

$$\cos(\epsilon) = \cos(\delta_1) \cdot \cos(\delta_\odot) + \sin(\delta_1) \cdot \sin(\delta_\odot) \cdot \cos(\alpha_1 - \alpha_\odot) = 0.73076 \quad \gg \gg \quad \epsilon \approx 43^\circ 3'$$

Distance from Earth:

Triangle Sun – Earth – Head of Comet (SEH)

Let's assume distance S-E $A = 1$ AU; S-H $R = 1.024$ AU; E-H $X = ?$

$$(R)^2 = X^2 + 1 - 2 \cdot X \cdot \cos(\epsilon) \quad \Rightarrow \quad X \approx 0.9 \text{ AU}$$

$$\sin(\epsilon)/R = \sin(\text{EHS}) / 1 \gg \gg \quad \text{Angle EHS} = 41.5^\circ$$

Linear size of head;

Assume that the head has a spherical shape

$$\text{Head radius } r_h / x = \tan(0.28^\circ/2) \gg \gg \quad r_h = 0.0022 \text{ AU} \approx 330\,000 \text{ km}$$

Linear size of tail (H-T)

From triangle Earth- Comet Head- comet tail's end (EHT)

$$\text{Angle EHT} = 180^\circ - \text{EHS} = 138.5^\circ$$

$$\text{Angle HET} = 2^\circ$$

$$\text{Angle HTE} = 39.5^\circ$$

$$X/\sin(39.5^\circ) = \text{H-T} / \sin(2^\circ) \gg \gg \quad \text{H-T} \approx 0.05 \text{ AU}$$

