

Data analysis – reserve: solution

Picture scale:

For example from stars C D > distance on picture = 63 ± 1 mm

From parallactic triangle or from map measurements distance C-D = $2.5^\circ = 150'$

Scale $150'/63 = 2.38'/\text{mm} \approx 0.04^\circ/\text{mm}$

Comet's Head size = 7 mm = 0.28°

Comet's tail size (end of tail should be marked by student) 50 mm = 2° (angle HET)

Coordinates of comet $\alpha_1 \approx 21h52' \delta_1 \approx 37.5^\circ$; $\alpha_2 \approx 22h03' \delta_1 \approx 38.8^\circ$

Angular speed $\approx 2.5^\circ/24h = 6.25'/\text{h}$

Elongation ε

$$\cos(\varepsilon) = \cos(\delta_1) \cdot \cos(\delta_2) + \sin(\delta_1) \cdot \sin(\delta_2) \cdot \cos(\alpha_1 - \alpha_2) = 0.73076 \quad \ggg \quad \varepsilon \approx 43^\circ 3'$$

Distance from Earth:

Triangle Sun – Earth – Head of Comet (SEH)

Let's assume distance S-E A = 1 AU; S-H R = 1.024 AU; E-H X =?

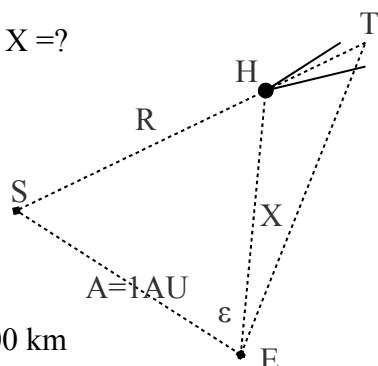
$$(R)^2 = X^2 + 1 - 2 \cdot X \cdot \cos(\varepsilon) \quad > \quad X \approx 0.9 \text{ AU}$$

$$\sin(\varepsilon)/R = \sin(EHS) / 1 \quad \ggg \quad \text{Angle EHS} = 41.5^\circ$$

Linear size of head;

Assume that the head has a spherical shape

$$\text{Head radius } r_h / x = \tan(0.28^\circ/2) \quad \ggg \quad r_h = 0.0022 \text{ AU} \approx 330 \, 000 \text{ km}$$



Linear size of tail (H-T)

From triangle Earth- Comet Head- comet tail's end (EHT)

Angle EHT = $180^\circ - EHS = 138.5^\circ$

Angle HET = 2°

Angle HTE = 39.5°

$$X/\sin(39.5^\circ) = H-T / \sin(2^\circ) \quad \ggg \quad H-T \approx 0.05 \text{ AU}$$