

Data Analysis Question 1 - solution

1) The star is a W UMa type, so both primary and secondary minima were observed. If the depth of the minimum isn't given, there is no way of deciding which (primary or secondary it is).

2) From the data, it can be seen that on four nights more than one minimum was observed. This allows us to estimate half the period based on the difference between pairs of observations:

minima	ΔT	average
2-1	.1367	$\Sigma/5 = .1367$ Period P = obtained average x 2 = 0.2734
4-3	.1372	
10-9	.1364	
11-10	.1373	
12-11	.1359	

3) For a first approximation of the elements, we chose an initial epoch (M_0), for example the first observed minimum 2454092.4111. The approximate elements are then:

$$M_{\text{calc}} = 2454092.4111 + 0.2734 * E$$

4) For an exact determination of the elements we draw an O-C diagram. The data for making the O-C diagram are calculated as follows:

No	(M_{obs}) 2454000 +	$E = (M_{\text{obs}} - M_0)/P$	E (rounded to the nearest whole or half integer)	M_{calc} 2454000.0 +	O-C = $M_{\text{obs}} - M_{\text{calc}}$
1	092.4111	0	0,0	092,4111	0,0000
2	092.5478	0,5	0,5	092,5478	0.0000
3	367.3284	1005,5497	1005,5	367,3148	0,0136
4	367.4656	1006,0516	1006,0	367,4515	0,0141
5	388.5175	1083,0519	1083,0	388,5033	0,0142
6	388.6539	1083,5508	1083,5	388,6400	0,0139
7	704.8561	2240,1061	2240,0	704,8271	0,0290
8	776.4901	2502,1178	2502,0	776,4579	0,0322
9	835.2734	2717,1262	2717,0	835,2389	0,0345
10	847.3039	2761,1295	2761,0	847,2685	0,0354
11	847.4412	2761,6316	2761,5	847,4052	0,0360
12	847.5771	2762,1287	2762,0	847,5419	0,0352

5) The O-C diagram should be plotted on graph paper

6) From the diagram, it can be seen that over 2762 epochs the value of (O-C) increased by 0.0355 days, therefore over one cycle (one epoch) the period was too short by:

$$0.0355/2762 = 0.0000129$$

and the estimated period P should be increased by this value. Taking into account that the graph can be read to 3 significant figures, the correction should also be to 3 significant figures.

$$P' = 0,2734 + 0,0000129 = 0,2734129$$

thus the corrected light elements of V1107 Cas are:

$$M_{\text{calc}} = 2454092.4111 + 0.2734129 * E$$

7) The correction of the period could also be determined directly from the table, using the mean value of O-C for the initial epoch ($E=0$; 0,5) and the final epochs ($E=2761$; 2761,5; 2762)

8) To calculate the ephemeris, we need to know the JD of a given day. Since dates and JD numbers are given in the observations, we can calculate that, for example on 1 January 2008 r. at 12:00 the JD was 2454467.0, while on 1 January 2011 at 12:00 it was 2455563.0.

Since 1 September 2011 is the 243-rd day of the year, thus at 12:00 on that day JD 2455806.0 begins.

9) On 1 September 2011 at 18:00 (JD 2455806.25) there have been 1713.8389 days czyli or 6268.3176 epochs since the initial epoch M_0 (2454092.4111). Thus the nearest (secondary) minimum which agrees with these elements will be:

$$JD\ 2454092.4111 + 0,2734129 * 6268,5 = 2455806,2999 = \underline{\underline{19^h\ 12^m\ UT}}$$

The next (primary) minimum will be :

$$JD\ 2454092.4111 + 0,2734129 * 6269 = 2455806.4366 = \underline{\underline{22^h\ 29^m\ UT}}$$

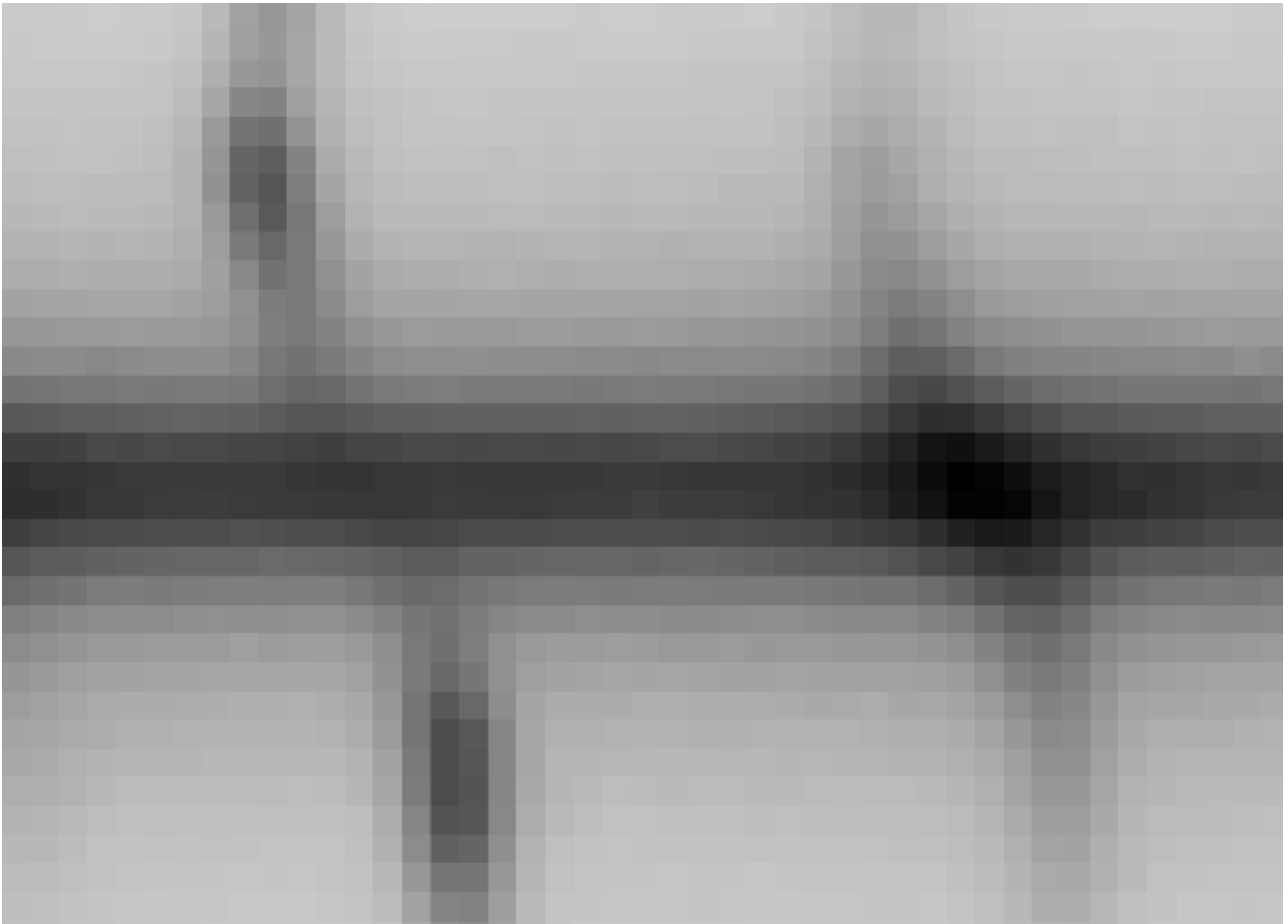
The next (secondary) minimum will be on the same night, at:

$$JD\ 2455806,4111 + 0,2734129 * 6269,5 = 2457520,5733$$

that is on 2 września at **1^h 46^m UT**

Earlier and later minima can be determined by adding or subtracting half a period, or 3^h17^m

Data Analysis Question 2 - solution



Solution:

$$\Delta\lambda = \lambda_1 - \lambda_2 = 20 \text{ \AA}$$

$$\text{distance on picture} = 22 \text{ pixels} \pm 2 \quad \rightarrow \quad \text{horizontal scale } 20/22 = 0.9091 \text{ \AA/pixel}$$

$$\text{Doppler shift from spectrum between upper and lower arm: } \Delta\lambda = 7 \text{ pixels} \pm 1 = 6.3636 \text{ \AA}$$

$$2V_{\text{radial}} = c \cdot \Delta\lambda/\lambda \quad (c \approx 300\,000 \text{ km/s}) = 290.8 \text{ km/s}$$

Inclination problem: (i – angle between line of sight and galactic disc)

$$\text{Size of galaxy image: } a = 11.5 \pm 0.5 \text{ cm, } b = 6.5 \pm 0.5 \text{ cm} \quad \rightarrow \quad i = \arcsin(b/a) \approx 35^\circ$$

$$\cos(i) = V_{\text{radial}} / V_{\text{rotation}} \quad \rightarrow \quad V_{\text{rotation}} = V_{\text{radial}} / 2\cos(35) = 216.7 \text{ km/s}$$

Vertical scale (pixel to distance-from-centre conversion)

$$\text{For 1 pixel: angle } 0.82'' \text{ corresponds to } 2 \cdot 40 \text{ Mpc} \cdot \tan(0.82''/2) = 159 \text{ pc in galactic distance}$$

Mass determination:

$$\text{From Kepler's law: } M = V^2 \cdot R / G$$

$$R \approx 10 \text{ pixel} = 1590 \text{ pc} \cdot 3.09 \cdot 10^{16} \text{ m/pc} = 4.9 \cdot 10^{19} \text{ m}$$

$$M = 3.4 \cdot 10^{40} \text{ kg} > 1.7 \cdot 10^{10} M_{\odot} \quad (M_{\odot} \approx 2 \cdot 10^{30} \text{ kg})$$